











## Language learning: What kind of evidence?

- Children listen to language [unsupervised]
- Children are corrected?? [supervised]
- Children observe language in context
- Children observe frequencies of language

Remember: Language = set of strings

#### Poverty of the Stimulus (1957)

**Chomsky:** Just like polynomials: never enough data unless you know something in advance. So kids must be born knowing what to expect in language.

- Children listen to language
- Children are corrected??
- Children observe language in context
- Children observe frequencies of language

## Gold's Theorem (1967)

a simple negative result along these lines: kids (or computers) can't learn much without supervision, inborn knowledge, or statistics

- Children listen to language
- Children are corrected??
- Children observe language in context
- Children observe frequencies of language

## The Idealized Situation

- Mom talks
- Baby listens
- 1. Mom outputs a sentence
- 2. Baby hypothesizes what the language is (given all sentences so far)
- 3. Goto step 1
- Guarantee: Mom's language is in the set of hypotheses that Baby is choosing among
- Guarantee: Any sentence of Mom's language is eventually uttered by Mom (even if infinitely many)
  - Assumption: Vocabulary (or alphabet) is finite.

# Can Baby learn under these conditions?

- Learning in the limit:
  - There is some point at which Baby's hypothesis is correct and never changes again. Baby has converged!
  - Baby doesn't have to know that it's reached this point it can keep an open mind about new evidence – but if its hypothesis is right, no such new evidence will ever come along.
- A class C of languages is learnable in the limit if one could construct a perfect C-Baby that can learn any language L ∈ C in the limit from a Mom who speaks L.
- Baby knows the class C of possibilities, but not L.
- Is there a perfect finite-state Baby?
- Is there a perfect context-free Baby?

# Languages vs. Grammars

- Does Baby have to get the right grammar?
- (E.g., does VP have to be called VP?)
- Assumption: Finite vocabulary.





#### Evil Mom

- To find out whether Baby is perfect, we have to see whether it gets 100% even in the most adversarial conditions
- Assume Mom is trying to fool Baby
  - although she must speak only sentences from L
    and she must eventually speak each such sentence
- Does Baby's strategy work?

## An Unlearnable Class

- Class of languages:
  - Let L<sub>n</sub> = set of all strings of length < n</p>
  - What is L<sub>0</sub>?
  - What is L<sub>1</sub>?
  - What is L<sub>∞</sub>?
    - If the true language is  $L_{\!\scriptscriptstyle \infty}\!,$  can Mom really follow rules?
    - Must eventually speak every sentence of  $L_{\!\scriptscriptstyle\infty}\!.$  Possible?
    - Yes: ε; a, b; aa, ab, ba, bb; aaa, aab, aba, abb, baa, ...
  - Our class is  $C = \{L_0, L_1, \dots, L_\infty\}$

# An Unlearnable Class

- Let L<sub>n</sub> = set of all strings of length < n</p>
  - What is L<sub>0</sub>?
  - What is L<sub>1</sub>?
  - What is L<sub>∞</sub>?
- Our class is  $C = \{L_0, L_1, \dots L_\infty\}$
- A perfect C-baby will distinguish among all of these depending on the input.
- But there is no perfect C-baby ...

# An Unlearnable Class

- Our class is  $C = \{L_0, L_1, \dots, L_\infty\}$
- Suppose Baby adopts conservative strategy, always picking smallest possible language in C.
- So if Mom's longest sentence so far has 75 words, baby's hypothesis is L<sub>76</sub>.
- This won't always work: What language can't a conservative Baby learn?

## An Unlearnable Class

- Our class is C = {L<sub>0</sub>, L<sub>1</sub>, ... L<sub>∞</sub>}
- Could a non-conservative baby be a perfect C-Baby, and eventually converge to any of these?
- Claim: Any perfect C-Baby must be "quasiconservative":
  - If true language is L<sub>76</sub>, and baby posits something else, baby must still eventually come back and guess L<sub>76</sub> (since it's perfect).
  - So if longest sentence so far is 75 words, and Mom keeps talking from L<sub>76</sub>, then eventually baby must actually return to the conservative guess L<sub>76</sub>.
  - Agreed?

## Mom's Revenge

If longest sentence so far is 75 words, and Mom keeps talking from  $L_{76}$ , then eventually a perfect C-baby must actually return to the conservative guess  $L_{76}$ .

- Suppose true language is L<sub>∞</sub>
- Evil Mom can prevent our supposedly perfect C-Baby from converging to it.
- If Baby ever guesses L<sub>∞</sub>, say when the longest sentence is 75 words:
  - Then Evil Mom keeps talking from L<sub>76</sub> until Baby capitulates and revises her guess to L<sub>76</sub> as any perfect C-Baby must.
     So Baby has *not* stayed at L<sub>w</sub> as required.
- Then Mom can go ahead with longer sentences. If Baby ever guesses L<sub>∞</sub> again, she plays the same trick again.

#### Mom's Revenge

If longest sentence so far is 75 words, and Mom keeps talking from  $L_{76}$ , then eventually a perfect C-baby must actually return to the conservative guess  $L_{76}$ .

- Suppose true language is L<sub>a</sub>
- Evil Mom can prevent our supposedly perfect C-Baby from converging to it.
- If Baby ever guesses  $L_{\infty}$ , say when the longest sentence is 75 words:
  - Then Evil Mom keeps talking from L<sub>76</sub> until Baby capitulates and revises her guess to L<sub>76</sub> – as any perfect C-Baby must.
  - So Baby has not stayed at L<sub>∞</sub> as required.
- Conclusion: There's no perfect Baby that is guaranteed to converge to L<sub>0</sub>, L<sub>1</sub>, ... or L<sub>∞</sub> as appropriate. If it always succeeds on finite languages, Evil Mom can trick it on infinite language.

#### Implications

- We found that C = {L<sub>0</sub>, L<sub>1</sub>, ... L<sub>∞</sub>} isn't learnable in the limit.
- How about class of finite-state languages?
  - Not unless you limit it further (e.g., # of states)
     After all, it includes all languages in C, and more, so learner has harder choice
- How about class of context-free languages?
   Not unless you limit it further (e.g., # of rules)

## Punchline

- But class of *probabilistic* context-free languages is learnable in the limit!!
- If Mom has to output sentences randomly with the appropriate probabilities,
  - she's unable to be too evil
  - there are then perfect Babies that are guaranteed to converge to an appropriate probabilistic CFG
- I.e., from hearing a finite number of sentences, Baby can correctly converge on a grammar that predicts an infinite number of sentences.
   Baby is generalizing! Just like real babies!



